

Generalized Interference Alignment—Part II: Application to Wireless Secrecy

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Abstract—In contrast to its wired counterpart, wireless communication is highly susceptible to eavesdropping due to the broadcast nature of the wireless propagation medium. Recent works have proposed the use of interference to reduce eavesdropping capabilities in wireless wiretap networks. However, the concurrent effect of interference on both eavesdropping receivers (ERs) and legitimate receivers has not been thoroughly investigated, and careful engineering of the network interference is required to harness the full potential of interference for wireless secrecy. This two-part article addresses this issue by proposing a generalized interference alignment (GIA) technique, which jointly designs the transceivers at the legitimate partners to impede the ERs without interfering with LRs. In Part I, we have established a theoretical framework for the GIA technique. In Part II, we will first propose an efficient GIA algorithm that is applicable to large-scale networks and then evaluate the performance of this algorithm in stochastic wireless wiretap network via both analysis and simulation. These results reveal insights into when and how GIA contributes to wireless secrecy.

Index Terms—MIMO, interference alignment, wireless secrecy.

I. INTRODUCTION

A. Background and Survey

CONFIDENTIAL exchange of messages securely in wireless networks has become increasingly important for the modern information society. In contrast to its wired counterpart, wireless transmission is highly susceptible to eavesdropping due to the broadcast nature of the wireless propagation medium [1]. Contemporary wireless security systems, based on cryptographic primitives, evolved from schemes developed for traditional wired applications. To overcome challenges associated with broadcast communication, one must augment contemporary wireless security techniques using strategies that exploit the intrinsic properties of the wireless propagation medium.

A key observation in exploiting these properties is that the broadcast nature generates contrasting effects: It makes the

secrecy information from a certain legitimate transmitter (LT) vulnerable to malicious interception, but at the same time enables other legitimate partners to impede the eavesdropping receivers (ERs) via *interference*. Therefore, interference emerges as a potentially valuable resource for wireless network secrecy [2], [3]. The idea of enhancing network secrecy through the use of interference has been investigated in several recent works, under the name of artificial noise [4], [5], artificial noise alignment [6], [7], friendly jamming [8], [9], or cooperative jamming [10]–[12]. A major challenge in utilizing interference to enhance secrecy is that while impeding the ERs, interference affects the LRs as well. Hence, without proper coordination, interference may be of little help or even harmful to wireless secrecy in some network configurations [8]. We envision that a greater secrecy gain will be achieved by simultaneously coordinating multiple legitimate partners such that aggregated interference causes negligible effects at the legitimate receivers (LRs) while impeding ERs. This motivates the need to develop coordinative interference engineering strategies for wireless wiretap networks, which will be referred to as wireless-tap networks.¹

Several secrecy-enhancing interference engineering strategies have been proposed for small networks with one LT [6]–[8] or one LR [9]–[12]. Coordinating aggregated interference from multiple LTs at multiple LRs imposes new challenges on secrecy transmission strategy design. A promising candidate to overcome this challenge is interference alignment (IA) [13]. A few studies have adopted the IA scheme proposed in [13] to promote wireless secrecy [14]–[16]. However, the scheme in [13] is based on infinite dimensional symbols that require time or frequency domain symbol extension, making it difficult to implement in practice.

To avoid the infinite dimension issue, researchers have developed spatial-domain IA techniques in which no symbol extension is involved and interference is coordinated and canceled via the finite signal dimension provided by multiple antennas [17]. In Part I, a theoretical framework has been established to address the two key issues of spatial-domain IA, i.e., feasibility conditions and transceiver design. Moreover, to further enhance the network's capability of secrecy protection, legitimate jammers (LJs) are incorporated to better impede ERs without interfering with the LRs. In this paper, this technique is referred to as generalized interference alignment (GIA). To apply the GIA technique to practical wireless-tap networks, the following issues need to be addressed:

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¹“Wireless wiretap” is referred to as “wireless-tap” to emphasize the wireless nature of the propagation medium.

- **Design of effective scalable GIA algorithms:** In large-scale networks, the limited policy space in transceiver design is insufficient to cancel interference on all cross links. Existing works applying IA to large-scale networks [18], [19] address this issue by first dividing a large network into small clusters and then performing IA separately on each cluster. However, under this approach, the inter-cluster interference is not addressed, and some of it may be the strongest interference perceived by the LRs on a cluster edge. On the other hand, if every LR wishes to cancel the strongest interference it perceives, the feasibility conditions of the entire network are coupled together, which normally requires centralized approaches that are not applicable to large networks. Hence, designing effective scalable GIA algorithms is difficult.
- **Characterization of the performance of GIA in stochastic networks:** To obtain insights into the performance of GIA in generic wireless-tap networks, it is desirable to characterize how GIA performs in large-scale stochastic wireless-tap networks. A few works have analyzed the performance of stochastic networks with interference control [20], [21]. In these works, the interference control policies at different nodes are independent. However, with GIA, the interference control policies at different LTs and LJs become correlated, making it difficult to quantify aggregate interference at LRs and ERs. Therefore, characterizing the performance of GIA in stochastic networks is challenging.

B. Contribution of This Work

In this work, we will address the challenges listed above. We consider MIMO wireless-tap networks with LJs. To enable the design of effective and scalable GIA algorithms, we first decompose the GIA feasibility conditions to a per-node basis. Based on that, we propose an algorithm that generates a feasible alignment set by only requiring each legitimate node to communicate with a few nodes, the number of which does not scale with the size of the network. This algorithm, together with the distributive GIA transceiver design algorithm proposed in Part I, construct a GIA algorithm that is applicable to large-scale wireless-tap networks. We then characterize the performance of the proposed algorithm in stochastic wireless-tap networks. We jointly adopt Cauchy-Schwarz inequality, Chebyshev inequality, and Chernoff inequality to bound the effect of aggregate interference from multiple correlated sources, and obtain the performance of GIA. This result demonstrates the contribution of GIA to network secrecy enhancement. It also illustrates how major network parameters, such as node density and antenna configuration, affect the performance of wireless-tap networks. We also perform various simulations to obtain insights into when and the how GIA technique benefits network secrecy.

C. Notations

The notations are consistent with Part I. Additional notations are listed in the following.

1) *Functions:* Function $[\cdot]^+ = \max\{\cdot, 0\}$, $\Gamma(\cdot)$ and $\Gamma(\cdot, \cdot)$ are the gamma function and incomplete gamma function, respectively, $\lfloor \cdot \rfloor$ denotes the floor function, and $(\cdot)^*$ denotes the complex conjugate of a matrix.

2) *Probability Theory:* The operators $\mathbb{E}\{\cdot\}$, $\mathbb{V}\{\cdot\}$, and $\mathbb{S}\{\cdot\}$ denote the expectation, variance, and standard deviation of a random variable, and $\mathbb{P}\{\cdot\}$ denotes the probability of an event. $\mathcal{N}_c(\mu, \sigma^2)$ represents complex Gaussian distribution, with mean μ and standard deviation σ .

II. PROBLEM FORMULATION

In this section, we first describe the system model of wireless-tap networks, then illustrate the potential benefits of GIA via a case study, and finally formulate the alignment set design problem of GIA.

A. System Model

Consider a network consisting of K LT-LR pairs, J LJs and K ERs (The LTs and LJs are indexed from 1 to K and from $K+1$ to $K+J$, respectively.). LT j (or LJ j , if $j > K$), LR k , and ER k are equipped with M_j , $N_k^{(\ell)}$, and $N_k^{(e)}$ antennas, respectively. At each time slot, LT (or LJ) j sends d_j independent symbols. LT k attempts to send confidential messages to LR k , while ER k attempts to intercept these messages. LJ j transmits dummy data to generate interference.

The received signals $\mathbf{y}_k^{(\ell)}, \mathbf{y}_k^{(e)} \in \mathbb{C}^{d_k}$ at LR k and ER k are given by

$$\mathbf{y}_k^{(\iota)} = (\mathbf{U}_k^{(\iota)})^\dagger \left(\mathbf{H}_{kk}^{(\iota)} \mathbf{V}_k \mathbf{x}_k + \sum_{j=1, \neq k}^{\tilde{K}} \mathbf{H}_{kj}^{(\iota)} \mathbf{V}_j \mathbf{x}_j + \mathbf{z}_k^{(\iota)} \right), \quad (1)$$

where $\tilde{K} = K + J$, $\mathbf{H}_{kj}^{(\iota)} \in \mathbb{C}^{N_k^{(\iota)} \times M_j}$, $\iota \in \{\ell, e\}$ are the channel matrices from LT (or LJ) j to LR k or ER k , whose entries are independent random variables drawn from continuous distributions; $\mathbf{x}_j \in \mathbb{C}^{d_j}$ is the encoded information symbol at LT (or LJ) j ; $\mathbf{V}_j \in \mathbb{C}^{M_j \times d_j}$ is the precoder at LT (or LJ) j ; $\mathbf{U}_k^{(\iota)} \in \mathbb{C}^{N_k^{(\iota)} \times d_k}$, $\iota \in \{\ell, e\}$ is the decoder at LR k or ER k ; and $\mathbf{z}_k^{(\iota)} \in \mathbb{C}^{N_k^{(\iota)} \times 1}$, $\iota \in \{\ell, e\}$ is the white Gaussian noise with zero mean and unit variance. The transmission power of LT (or LJ) j is given by $P_j = \mathbb{E}\{\text{Tr}(\mathbf{x}_j^\dagger \mathbf{V}_j^\dagger \mathbf{V}_j \mathbf{x}_j)\}$. Define the configuration of the legitimate network as $\mathcal{X} \triangleq \{(M_1, M_2, \dots, M_{\tilde{K}}), (N_1^{(\ell)}, N_2^{(\ell)}, \dots, N_K^{(\ell)}), (d_1, d_2, \dots, d_{\tilde{K}})\}$.

This work adopts Information-theoretic security as the performance metric. From [22], [23], under a given transceiver design, the following secrecy rate R_k^S is achievable for legitimate link k :

$$R_k^S = \mathbb{E}\{[r_k^{(\ell)} - r_k^{(e)}]^+\}, \quad (2)$$

in which $r_k^{(\iota)}$, $\iota \in \{\ell, e\}$, is given by

$$r_k^{(\iota)} = \log_2 \det \left\{ \mathbf{I} + (\mathbf{U}_k^{(\iota)})^\dagger \mathbf{H}_{kk}^{(\iota)} \mathbf{V}_k (\mathbf{H}_{kk}^{(\iota)} \mathbf{V}_k)^\dagger \mathbf{U}_k^{(\iota)} \right. \\ \left. \left[(\mathbf{U}_k^{(\iota)})^\dagger \left(\mathbf{I} + \sum_{j=1, \neq k}^{\tilde{K}} \mathbf{H}_{kj}^{(\iota)} \mathbf{V}_j (\mathbf{H}_{kj}^{(\iota)} \mathbf{V}_j)^\dagger \right) \mathbf{U}_k^{(\iota)} \right]^{-1} \right\}. \quad (3)$$

From [15], when the transmission power at all LTs and LJs are of the same order, i.e., for some $\theta_1, \theta_h > 0$, $\frac{P_j}{P} \in [\theta_1, \theta_h]$, $\forall j$, the secure degree of freedom (sDoF) can be defined as

$$D_k^S = \lim_{P \rightarrow \infty} \frac{R_k^S}{\log_2(P)}. \quad (4)$$

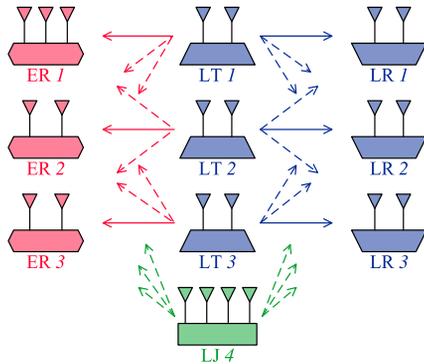


Fig. 1. Configuration of the example network.

B. Case Study

Example: As illustrated in Fig. 1, consider a MIMO wireless-tap network, as described in Section II-A, with $K = 3$, $J = 1$, antenna configuration $M_k = N_k^{(\ell)} = 2$, $k \in \{1, 2, 3\}$, $M_4 = 4$, $N_1^{(e)} = 3$, $N_2^{(e)} = N_3^{(e)} = 2$, and data stream configuration $d_k = 1$, $k \in \{1, 2, 3, 4\}$. The entries of all the channel matrices are independent random variables drawn from $\mathcal{N}_c(0, 1)$. The transmit power at all nodes is 20 dB, i.e., $P_k = P = 100$, $k \in \{1, 2, 3, 4\}$. \square

Compare four different strategies: the first two are non-cooperative, whereas the other two are cooperative:

- Zero forcing with 2 active LTs:* LT 1, 2 use random precoders $\mathbf{v}_1, \mathbf{v}_2$,² and LR 1, 2 use zero forcing to cancel interference, i.e., $\mathbf{u}_1^{(\ell)} = \mathbf{Z}(\mathbf{H}_{12}^{(\ell)} \mathbf{v}_2)^*$ and $\mathbf{u}_2^{(\ell)} = \mathbf{Z}(\mathbf{H}_{21}^{(\ell)} \mathbf{v}_1)^*$, where $\mathbf{Z} = \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$. To avoid interfering with LR 1 and 2, LT 3 and LJ 4 remain silent, i.e., $\mathbf{v}_3 = \mathbf{0}$, $\mathbf{v}_4 = \mathbf{0}$.
- Zero forcing with 3 active LTs:* LT 1, 2 and 3 use random precoders $\mathbf{v}_1, \mathbf{v}_2$ and \mathbf{v}_3 , and LR 1, 2 and 3 use zero forcing to cancel interference from LT 2, 3 and 1, respectively, i.e., $\mathbf{u}_1^{(\ell)} = \mathbf{Z}(\mathbf{H}_{12}^{(\ell)} \mathbf{v}_2)^*$, $\mathbf{u}_2^{(\ell)} = \mathbf{Z}(\mathbf{H}_{23}^{(\ell)} \mathbf{v}_3)^*$ and $\mathbf{u}_3^{(\ell)} = \mathbf{Z}(\mathbf{H}_{31}^{(\ell)} \mathbf{v}_1)^*$. LJ 4 remains silent.
- IA:* LT 1–3 adopt IA to design precoders $\{\mathbf{v}_k\}$. Interference at every LR is aligned into a 1-dimensional subspace. Specifically, \mathbf{v}_1 is designed to be an eigenvector of $(\mathbf{H}_{31}^{(\ell)})^{-1} \mathbf{H}_{32}^{(\ell)} (\mathbf{H}_{12}^{(\ell)})^{-1} \mathbf{H}_{13}^{(\ell)} (\mathbf{H}_{23}^{(\ell)})^{-1} \mathbf{H}_{21}^{(\ell)}$, $\mathbf{v}_2 = (\mathbf{H}_{32}^{(\ell)})^{-1} \mathbf{H}_{31}^{(\ell)} \mathbf{v}_1$, and $\mathbf{v}_3 = (\mathbf{H}_{23}^{(\ell)})^{-1} \mathbf{H}_{21}^{(\ell)} \mathbf{v}_1$. $\mathbf{u}_1^{(\ell)}$, $\mathbf{u}_2^{(\ell)}$, and $\mathbf{u}_3^{(\ell)}$ are designed as in Strategy B. LJ 4 still remains silent.
- GIA:* LT 1–3 and LJ 4 adopt a coordinated approach to design their precoders so that interference at every LR is aligned to a 1-dimensional subspace. Specifically, the LTs and LR design their transceivers as in Strategy C. LJ 4 designs \mathbf{v}_4 so that $\mathbf{v}_4 \perp ((\mathbf{u}_k^{(\ell)})^\dagger \mathbf{H}_{k4}^{(\ell)})^T$, $k \in \{1, 2, 3\}$. This design is feasible as $((\mathbf{u}_k^{(\ell)})^\dagger \mathbf{H}_{k4}^{(\ell)})^T$, $k \in \{1, 2, 3\}$ are three vectors in \mathbb{C}^4 .

The signal space at LR 1, 2 and ER 1, 2, as well as the secrecy rate and sDoF of LR 1, 2 under the above four strategies, are illustrated and compared in Fig. 2.³ From this figure, Strategy

²Small letters are used for all transceivers as they are vectors in this example.

³Because the cases of LR 3/ER 3 are identical to those of LR 2/ER 2 under Strategy B-D, they are omitted in Fig. 2 for conciseness.

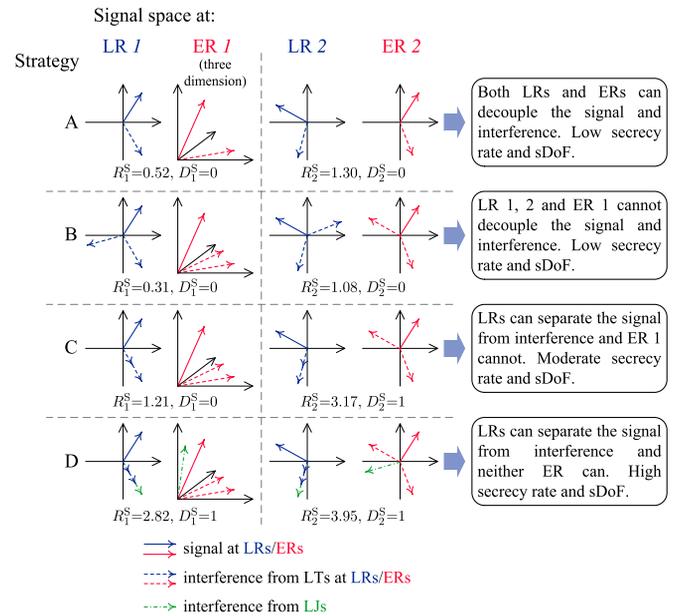


Fig. 2. Signal space at LR 1, 2 and ER 1, 2 under different strategies.

C, D perform better than Strategy A, B. This is because the channel states between LTs and LR $\{\mathbf{H}_{kj}^{(\ell)}\}$ are independent of those between LTs and ER $\{\mathbf{H}_{kj}^{(e)}\}$. Therefore, interference that is aligned at the LR is not aligned at the ER almost surely. This fact allow the legitimate network to impede ERs without affecting LR. Strategy D performs best as its jointly exploits the capability of all legitimate partners, i.e., LTs, LR, and LJ, to generate desirable interference.

Remark 2.1 (Practical Issues): It is worth noting that the GIA technique proposed in the example

- **Requires no channel state for the eavesdropping link.** The transceivers of the legitimate partners are functions of the channel state of legitimate links, i.e., $\{\mathbf{H}_{kj}^{(\ell)}\}$. In other words, no channel state information (CSI) of the eavesdropping link, i.e., $\{\mathbf{H}_{kj}^{(e)}\}$ is required.
- **Is effective even if ERs have all the CSI.** The performance of Strategy D comes from the unequal dimension of the interference at the ERs and LR. Since this property is due to the fact that the two sets of channel state $\{\mathbf{H}_{kj}^{(\ell)}\}$ and $\{\mathbf{H}_{kj}^{(e)}\}$ are independent, it is invariant with respect to the amount of CSI at the ERs.

These properties greatly improve the practicality of the proposed GIA technique. For instance, the possible leakage of CSI from the legitimate network to ERs does not affect the performance of the proposed algorithms. \square

C. Alignment Set Design

In Section II-B, the potential of GIA technique in secrecy enhancement is demonstrated. To cope with the general cases, the following problem is addressed in Part I:

Problem 2.1 (GIA Transceiver Design): Design transceivers $\{\mathbf{U}_k^{(\ell)}, \mathbf{V}_j\}$, $k \in \{1, 2, \dots, K\}$, $j \in \{1, 2, \dots, \bar{K}\}$ that satisfy the following constraints:

$$\text{Rn}((\mathbf{U}_k^{(\ell)})^\dagger \mathbf{H}_{kk}^{(\ell)} \mathbf{V}_k) = d_k, \quad \forall k \in \{1, 2, \dots, K\}, \quad (5)$$

$$\text{Rn}(\mathbf{V}_j) = d_j, \quad \forall j \in \{K+1, K+2, \dots, \tilde{K}\}, \quad (6)$$

$$\text{and } (\mathbf{U}_k^{(\ell)})^\dagger \mathbf{H}_{k,j}^{(\ell)} \mathbf{V}_j = \mathbf{0}, \quad \forall (k, j) \in \mathcal{A}, \quad (7)$$

where $\mathcal{A} \subseteq \mathcal{A}_{\text{all}} = \{(k, j) : k \in \{1, 2, \dots, K\}, j \in \{1, 2, \dots, \tilde{K}\}, k \neq j\}$ is the *alignment set*. It characterizes the set of interference to be canceled by GIA. \square

In Part I, the feasibility conditions of Problem 2.1 are analyzed for given network configuration χ and alignment set \mathcal{A} . In practice, the network configuration is usually fixed *a priori*. Hence, to design feasible GIA strategies, the following problem needs to be addressed:

Problem 2.2 (Alignment Set Design): Design \mathcal{A} so that GIA is feasible, i.e., Problem 2.1 has solutions. \square

To develop GIA techniques that are applicable to large-scale networks, it is important to design algorithms that can solve Problem 2.2 distributively. However, this task is difficult due to the following technical challenge.

Challenge of Coupled Feasibility Conditions

As Corollary 4.3 of Part I shows, for GIA to be feasible, it is necessary that the number of variables in transceiver design is no less than the number of constraints for *all* subsets of GIA constraints in (7). This fact illustrates that GIA feasibility conditions are inherently coupled with each other. Since there are exponentially many subsets of GIA constraints, the design of a feasible alignment set is complicated.

III. ALGORITHM DESIGN

In this section, a GIA algorithm is proposed to solve Problem 2.2 distributively.

Definition 1 (Proper Alignment Subsets): Alignment subsets $\mathcal{A}^{(r)}(k) = \{(k, j)\} \subseteq \{k\} \times (\{\tilde{K}\} \setminus \{k\})$, and

$$\mathcal{A}^{(t)}(j) = \{(k, j)\} \subseteq (\{1, 2, \dots, K\} \setminus \{j\}) \times \{j\}$$

are *proper* iff

$$\sum_{\substack{j:(k,j) \in \\ \mathcal{A}^{(r)}(k)}} d_j \leq N_k^{(\ell)} - d_k, \quad \sum_{\substack{k:(k,j) \in \\ \mathcal{A}^{(t)}(j)}} d_k \leq M_j - d_j. \quad (8)$$

\square

Theorem 3.1 (Proper Alignment Subsets Lead to GIA Feasibility): Problem 2.1 is feasible almost surely if the alignment set \mathcal{A} can be covered by proper alignment subsets, i.e.,

$$\mathcal{A} = \left(\bigcup_{k \in \{1, 2, \dots, K\}} \mathcal{A}^{(r)}(k) \right) \cup \left(\bigcup_{j \in \{1, 2, \dots, \tilde{K}\}} \mathcal{A}^{(t)}(j) \right) \quad (9)$$

for some proper alignment subsets $\mathcal{A}^{(r)}(k)$ and $\mathcal{A}^{(t)}(j)$.

Proof: Please refer to Appendix A for the proof. \square

Solution to Coupled Feasibility Conditions

Since (8) is a set of per-node constraints, Theorem 3.1 provides a mechanism to decompose the GIA feasibility constraints to a per-node basis. This result enables legitimate nodes to distributively design the alignment set, while maintaining the GIA feasibility.

Based on Theorem 3.1, the following algorithm is adopted to generate alignment set \mathcal{A} .

Algorithm 1 (Generate Feasible Alignment Set)

- **Alignment set selection at the transmitter side:** LT (or LJ) j selects a few LRs such that $\mathcal{A}^{(t)}(j)$ satisfies (8).⁴ Notify the selected LRs.
 - **Alignment set selection at the receiver side:** LR k selects among the transmitters which do not select LR k in the previous step, and make $\mathcal{A}^{(r)}(k)$ satisfy (8).
 - **Generate alignment set:** Set \mathcal{A} according to (9). \square
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Corollary 3.1 (Feasibility of Algorithm 1): In a MIMO wireless-tap network, when the alignment set \mathcal{A} is generated by Algorithm 1, Problem 2.1 is feasible almost surely.

Proof: This is a direct consequence of Theorem 3.1. \square

Remark 3.1 (Scalable GIA Algorithm): The freedom in designing the alignment subsets, $\mathcal{A}^{(t)}(j)$, $\mathcal{A}^{(r)}(k)$ in Algorithm 1 enables the legitimate nodes to distributively select the strongest interfering links and hence effectively manage interference. By first performing Algorithm 1 to design a feasible alignment set \mathcal{A} and then using the algorithm proposed in Part I to design the transceivers $\{\mathbf{U}_k^{(\ell)}, \mathbf{V}_j\}$, a distributive GIA algorithm is obtained. In this algorithm, the number of nodes that each node needs to exchange messages with are determined by the alignment subsets and hence does not scale with the size of the network. \square

IV. PERFORMANCE ANALYSIS

In this work, homogeneous Poisson point process (PPP) [24] will be employed to model the spatial distribution of stochastic wireless networks.

Definition 2 (Stochastic Wireless-Tap Network):

- *Channel Model:* The nodes are distributed in a two-dimensional infinite plane \mathbb{R}^2 . The channel state between two nodes positioned at $\mathbf{a}, \mathbf{b} \in \mathbb{R}^2$ is given by

$$\mathbf{H}_{\mathbf{a}, \mathbf{b}} = L(\mathbf{a}, \mathbf{b}) \tilde{\mathbf{H}}_{\mathbf{a}, \mathbf{b}},$$

where the elements in $\tilde{\mathbf{H}}$ are independent random variables following complex Gaussian distribution with zero mean and unit variance and the pathloss

$$L(\mathbf{a}, \mathbf{b}) = \|\mathbf{a} - \mathbf{b}\|^{-\frac{\alpha}{2}} \mathbb{1} \{ \|\mathbf{a} - \mathbf{b}\|^{-\frac{\alpha}{2}} \geq \theta \}, \quad (10)$$

where $\alpha \in [2, 4]$ is the pathloss exponent and θ is the cutoff threshold.⁵

- *Legitimate user network:* The position of the LTs is modeled by a homogeneous PPP with density $\lambda^{(\ell)}$. For an LT located at \mathbf{b} , the position of the associated LR is given by $\mathbf{a} = \mathbf{b} + \mathbf{p}_{\mathbf{b}}$, where $\mathbf{p}_{\mathbf{b}}$ is drawn from certain probability

⁴Here node selection criteria is not specified as it does not affect the feasibility of the alignment set. The selection criteria will be specified in the next section to enable performance analysis.

⁵Suppose the maximum transmit power of nodes in the network is P_{max} . Then when $\theta^2 P_{\text{max}} \ll 1$, the interference that has been ignored by the pathloss cutoff threshold is insignificant compared to white noise. In this case, the pathloss model in (10) is a reasonable approximation of the classical one. The two models will be compared via simulation in Fig. 7.

distribution in \mathbb{R}^2 , with $\|\mathbf{p}_b\| \leq \theta^{-\frac{2}{\alpha}}$.⁶ Each LR and LT is equipped with $M^{(\ell)}$ and $N^{(\ell)}$ number of antennas, respectively. Each LT delivers $d^{(\ell)} (\leq \min\{M^{(\ell)}, N^{(\ell)}\})$ independent data streams. Denote $\mathbf{p}_a = -\mathbf{p}_b$.

- *Legitimate jammer network:* The position of the LJs is modeled by a PPP with density $\lambda^{(j)}$. Each LJ has $M^{(j)}$ number of antennas and delivers $d^{(j)} (\leq M^{(j)})$ independent dummy data streams.
- *Eavesdropper network:* The position of the ER attempting to intercept the information from the LT at position \mathbf{b} is given by $\mathbf{e} = \mathbf{b} + \tilde{\mathbf{p}}_b$, where $\tilde{\mathbf{p}}_b$ is drawn from certain probability distribution in \mathbb{R}^2 , with $\|\tilde{\mathbf{p}}_b\| \leq \theta^{-\frac{2}{\alpha}}$. Each ER is equipped with $N^{(e)}$ number of antennas and adopts minimum mean square error decoder. Denote $\mathbf{p}_e = -\tilde{\mathbf{p}}_b$. \square

In the following, the position of a node will be used to replace its index. For example, an LT positioned at $\mathbf{b} \in \mathbb{R}^2$ is denoted by LT \mathbf{b} . The set of the positions of LTs, LRs, LJs, and ERs are denoted by $\mathcal{T}^{(\ell)}$, $\mathcal{R}^{(\ell)}$, $\mathcal{T}^{(j)}$, and $\mathcal{R}^{(e)}$, respectively.

To cancel the strongest interference that each LR perceives, the selection criteria in Algorithm 1 is specified to enable the nodes to select their nearest neighboring nodes, i.e.,

- **Transmitter side:** LT \mathbf{b} sets $\mathcal{A}^{(t)}(\mathbf{b}) = \{(\mathbf{a}, \mathbf{b})\}$, where $\mathbf{a} \in \mathcal{R}^{(\ell)} \setminus \{\mathbf{b} + \mathbf{p}_b\}$, so that

$$L(\mathbf{a}, \mathbf{b}) \geq L(\tilde{\mathbf{a}}, \mathbf{b}), \quad \forall \tilde{\mathbf{a}} \in \mathcal{R}^{(\ell)} \setminus \mathcal{R}(\mathbf{b}), \quad (11)$$

$$|\mathcal{A}^{(t)}(\mathbf{b})| = \left\lfloor \frac{M^{(x)} - d^{(x)}}{d^{(\ell)}} \right\rfloor \triangleq m^{(x)}, \quad (12)$$

where $\mathcal{R}(\mathbf{b}) = \{\mathbf{a} : (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(t)}(\mathbf{b})\} \cup \{\mathbf{b} + \mathbf{p}_b\}$, and $x = \ell, j$ for the LTs and LJs, respectively.

- **Receiver side:** LR \mathbf{a} sets

$$\mathcal{A}^{(r)}(\mathbf{a}) = \{(\mathbf{a}, \mathbf{b}^{(\ell)})\} \cup \{(\mathbf{a}, \mathbf{b}^{(j)})\},$$

where $\mathbf{b}^{(\ell)} \in \mathcal{T}^{(\ell)} \setminus \{\mathbf{a} + \mathbf{p}_a\}$, $\mathbf{b}^{(j)} \in \mathcal{T}^{(j)}$, so that

$$(\mathbf{a}, \mathbf{b}^{(x)}) \notin \mathcal{A}^{(t)}(\mathbf{b}^{(x)}), \quad x \in \{\ell, j\}, \quad (13)$$

$$L(\mathbf{a}, \mathbf{b}^{(x)}) \geq L(\mathbf{a}, \mathbf{b}), \quad \forall \mathbf{b} \in (\mathcal{T}^{(\ell)} \cup \mathcal{T}^{(j)}) \setminus \mathcal{T}(\mathbf{a}), \quad (14)$$

$$N^{(\ell)} - d^{(\ell)} - \max\{d^{(\ell)}, d^{(j)}\} + 1 \leq d^{(\ell)} |\{(\mathbf{a}, \mathbf{b}^{(\ell)})\}| + d^{(j)} |\{(\mathbf{a}, \mathbf{b}^{(j)})\}| \leq N^{(\ell)} - d^{(\ell)} \quad (15)$$

where

$$\mathcal{T}(\mathbf{a}) = \{\mathbf{b} : (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a}) \cup \mathcal{A}^{(t)}(\mathbf{b})\} \cup \{\mathbf{a} + \mathbf{p}_a\}.$$

Define the *connection density* of the legitimate network and the jammer network $\rho^{(\ell)}$, $\rho^{(j)}$, as the expected number of LTs or LJs that may interfere with a receiver, i.e.,

$$\rho^{(\ell)} = \mathbb{E} \left\{ \sum_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\} \right\} = \pi \theta^{-\frac{4}{\alpha}} \lambda^{(\ell)}, \quad (16)$$

$$\rho^{(j)} = \mathbb{E} \left\{ \sum_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\} \right\} = \pi \theta^{-\frac{4}{\alpha}} \lambda^{(j)}, \quad (17)$$

⁶Otherwise, from (10), the channel between the LR and the associated LT is 0, which leads to a trivial result. For the same reason, the distance between LT and the corresponding ER is limited.

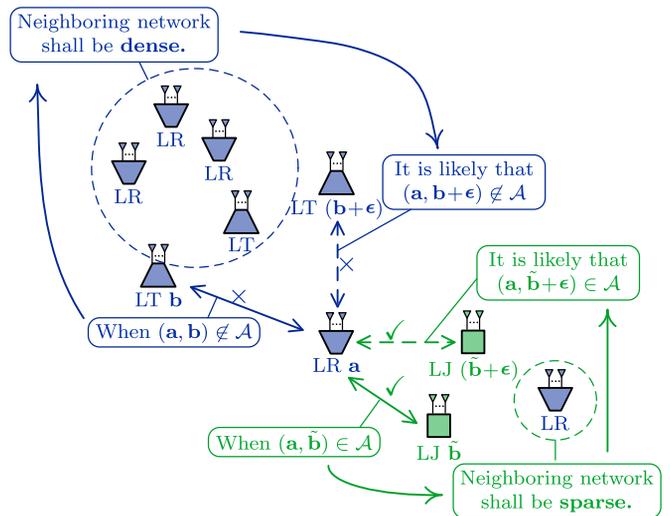


Fig. 3. Illustration of the correlation between alignment subsets of neighboring nodes. Consider two LTs (or LJs) positioned at \mathbf{b} and $\mathbf{b} + \boldsymbol{\epsilon}$, respectively, where $\boldsymbol{\epsilon} \in \mathbb{R}^2$ has a small norm. Events $(\mathbf{a}, \mathbf{b}) \in \mathcal{A}$ and $(\mathbf{a}, \mathbf{b} + \boldsymbol{\epsilon}) \in \mathcal{A}$ are correlated as the two transmitters perceive similar neighboring networks.

where $\mathbf{a} \in \mathbb{R}^2$.

This section focuses on analyzing the sDoF achieved by an LR. Firstly, a lemma which relates the sDoF to the dimension of interference at the LRs and ERs is proved.

Lemma 4.1 (Dimension of Interference): For LR \mathbf{a} with corresponding ER \mathbf{e} , the sDoF defined in (4) is given by

$$D^S = \left[\dim(\mathcal{S}^{(\ell)}) - \dim(\mathcal{S}^{(e)}) \right]^+, \quad (18)$$

where $\mathcal{S}^{(\iota)}$, $\iota \in \{\ell, e\}$ is a subspace of the receiving signal space of LR or ER, i.e., $\text{span}(\mathbf{U}_a^{(\ell)})$ or $\text{span}(\mathbf{U}_e^{(e)})$ that has no interference. Define $S^{(\iota)} \triangleq \dim(\mathcal{S}^{(\iota)})$, $\iota \in \{\ell, e\}$, then

$$S^{(\ell)} = \left[d^{(\ell)} - d^{(\ell)} \sum_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0 \ \& \ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}\} - d^{(j)} \sum_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0 \ \& \ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}\} \right]^+, \quad (19)$$

$$S^{(e)} = \min \left\{ d^{(\ell)}, \left[N^{(e)} - d^{(\ell)} \sum_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\} - d^{(j)} \sum_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\} \right]^+ \right\}. \quad (20)$$

Proof: Please refer to Appendix B for the proof. \square

From Lemma 4.1, to analyze the network's sDoF, the characterization of $S^{(\ell)}$ is necessary. However, this is challenging for the following reason.

Challenge of Correlated Alignment Set Selection

As illustrated in Fig. 3, events $(\mathbf{a}, \mathbf{b}) \in \mathcal{A}$ and $(\mathbf{a}, \mathbf{b} + \boldsymbol{\epsilon}) \in \mathcal{A}$ in the figure, are correlated. This example shows that the random variables $\mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0 \ \& \ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}\}$ in (19) are correlated for different \mathbf{b} . This correlation makes it difficult to characterize $S^{(\ell)}$.

This challenge is addressed by the following lemma.

Lemma 4.2 (Characterization of $S^{(\ell)}$): For LR \mathbf{a} , define

$$I^{(\ell)} \triangleq d^{(\ell)} \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(\ell)} \\ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(\ell)}(\mathbf{b})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\} \\ + d^{(j)} \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(j)} \\ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(j)}(\mathbf{b})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\}, \quad (21)$$

$$\varepsilon \triangleq N^{(\ell)} - d^{(\ell)} - d^{(\ell)} |\{\mathbf{b} \in \mathcal{T}^{(\ell)} : (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a})\}| \\ - d^{(j)} |\{\mathbf{b} \in \mathcal{T}^{(j)} : (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a})\}|. \quad (22)$$

Then

$$S^{(\ell)} = \min \left\{ d^{(\ell)}, [N^{(\ell)} - I^{(\ell)} - \varepsilon]^+ \right\}. \quad (23)$$

Moreover, ε is bounded within $[0, \max\{d^{(j)}, d^{(\ell)}\} - 1]$,

$$\mathbb{E}\{I^{(\ell)}\} \in \left[\sum_{x \in \{\ell, j\}} \left[\rho^{(x)} d^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)} d^{(x)} \right]^+, \right. \\ \left. \sum_{x \in \{\ell, j\}} \left[\rho^{(x)} d^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)} d^{(x)} \right]^+ \right. \\ \left. + \frac{d^{(x)} \lambda^{(x)} \sqrt{\rho^{(\ell)}}}{\lambda^{(\ell)} \sqrt{2\pi}} \right], \quad (24)$$

$$S\{I^{(\ell)}\} \leq \sum_{x \in \{\ell, j\}} \frac{4\lambda^{(x)} \sqrt{\pi \min\{m^{(x)}, \rho^{(\ell)}\}}}{\lambda^{(\ell)}} \\ \times \left(1 + \frac{1}{6 \min\{m^{(x)}, \rho^{(\ell)}\}} \right). \quad (25)$$

Proof: Please refer to Appendix C for the proof. \square

Solution to Correlated Alignment Set Selection

From (23), the major randomness of $S^{(\ell)}$ comes from that of $I^{(\ell)}$. Equations (24) and (25) show that the expectation of $I^{(\ell)}$ scales at $\mathcal{O}(\rho^{(\ell)})$, while its uncertainty in expectation and standard deviation both scale at $\mathcal{O}(\sqrt{\rho^{(\ell)}})$. Therefore, when $\rho^{(\ell)}$ is large, the randomness in $I^{(\ell)}$ can be ignored compared to its expectation, i.e., $\lim_{\rho^{(\ell)} \rightarrow +\infty} \frac{I^{(\ell)}}{\mathbb{E}\{I^{(\ell)}\}} = 1$. As will be discussed further in Remark 4.1, this property bounds the effect of correlated alignment set selection and enables an asymptotically accurate characterization of the sDoF performance.

Based on Lemma 4.2, the following theorem characterizes the sDoF of the GIA algorithm in a stochastic network.

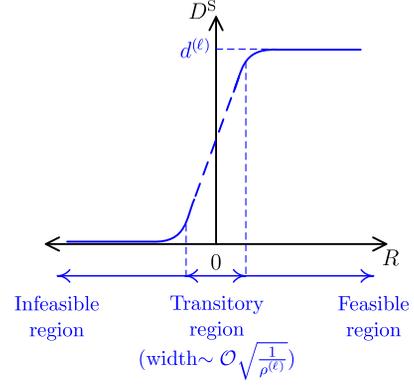


Fig. 4. Illustration of the sDoF per node described by (27).

Theorem 4.1 (Performance of GIA Algorithm): Indicator $R \in \mathbb{R}$ is defined in (26) at the bottom of the page. When $\rho^{(\ell)} \geq 1$ and $|R| > \sqrt{\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)})^2 d^{(\ell)}}}$, the sDoF per node $D^S \in [0, d^{(\ell)}]$ is given by

$$d^{(\ell)} \left[\mathbb{1}\{R > 0\} + \mathcal{O} \left(\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)} R)^2 d^{(\ell)}} \right) \right], \quad (27)$$

where $m^{(\ell)}, m^{(j)}$ are defined in (12).

Proof: Please refer to Appendix D for the proof. \square

Remark 4.1 (Interpretation of Theorem 4.1): Fig. 4 gives an intuitive illustration of the meaning of the sDoF expression in (27). This expression partitions the operation region into three parts according to the value of the indicator R . The sDoF per LR D^S is close to the upper bound $d^{(\ell)}$ in the feasible region, whereas it is close to the lower bound 0 in the infeasible region. Since the width of the transitory region is on $\mathcal{O}(\sqrt{\frac{1}{\rho^{(\ell)}}})$, (27) is asymptotically accurate when $\rho^{(\ell)} \rightarrow \infty$. This trend will be shown via simulation in Fig. 8. \square

In practice, it is interesting to understand how a stochastic wireless-tap network performs under various network parameters. However, as data stream numbers $d^{(\ell)}, d^{(j)}$ must be integers, and (26) contains the discontinuous function $[\cdot]$, it is difficult to obtain simple insights. To address this issue, a network with high connection density, i.e., $\rho^{(\ell)} \gg 1$, is analyzed in Appendix E. In this scenario, the width of the transitory region is ignorable, and hence sDoF per node $D^S = d^{(\ell)}$ when indicator $R > 0$. Define the set of feasible data streams as $\{(d^{(j)}, d^{(\ell)}) : R > 0\}$. Insights obtained from analysis on the feasible set are summarized as follows.

Remark 4.2 (Operation Modes of GIA): As illustrated in Fig. 5, in a wireless-tap network with high connection density,

$$R = \min \left\{ 1 - \frac{N^{(e)}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}}, \frac{N^{(\ell)} - d^{(\ell)} + \min\{m^{(\ell)} d^{(\ell)}, \rho^{(\ell)} d^{(\ell)}\} + \min\left\{\frac{\rho^{(j)}}{\rho^{(\ell)}} m^{(j)} d^{(j)}, \rho^{(j)} d^{(j)}\right\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} - 1 \right\}. \quad (26)$$

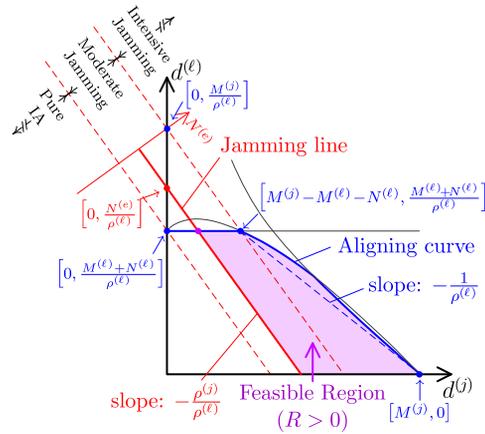


Fig. 5. Analysis of the feasible region of a stochastic wireless-tap network with high connection density. In this figure, $M^{(j)} \geq M^{(l)} + N^{(l)}$.

the set of feasible streams is contained by the region above the jamming line and below the aligning curve. The jamming line means that LTs and LJs have generated just enough interference to occupy the signal space of the ERs, and the aligning curve indicates that the LTs, LJs, and LR are on the cutting edge of being able to align all interference at the LR. The slope and the intersection of the jamming line are $-\frac{\rho^{(j)}}{\rho^{(l)}}$ and $\frac{N^{(e)}}{\rho^{(l)}}$, respectively. The aligning curve is a combination of a horizontal line and two second order curves. In particular, when $M^{(j)} \geq M^{(l)} + N^{(l)}$, the trapezoid with vertices $(0,0)$, $(0, \frac{M^{(l)} + N^{(l)}}{\rho^{(l)}})$, $(M^{(j)} - M^{(l)} - N^{(l)}, \frac{M^{(l)} + N^{(l)}}{\rho^{(l)}})$ and $(M^{(j)}, 0)$ lies below the aligning curve. From Fig. 5, GIA has three operation modes:

- **Pure IA mode:** When $N^{(e)} \leq N^{(l)} + M^{(l)}$, the LTs and LR can generate sufficient interference to jam the ERs and align all interference at the LR. The LJs can remain idle without losing optimality in the sDoF sense.
- **Moderate Jamming mode:** When

$$N^{(l)} + M^{(l)} < N^{(e)} \leq \max\{M^{(j)}, N^{(l)} + M^{(l)}\},$$

by adopting a small $d^{(j)}$, the LJs can help the LTs to jam the ERs without reducing the sDoF per LR.

- **Intensive Jamming mode:** When

$$N^{(e)} > \max\{M^{(j)}, N^{(l)} + M^{(l)}\},$$

the LJs need to adopt a large $d^{(j)}$ to generate sufficient interference to jam the ERs. As large $d^{(j)}$ is adopted, the sDoF per LR $d^{(l)}$ needs to be reduced so as to align the interference at the LR. \square

Remark 4.3 (Role of Network Parameters): The effects of network parameters on sDoF are summarized below.

- **LJ density $\rho^{(j)}$:** As Fig. 6(a) shows, larger $\rho^{(j)}$ leads to a steeper jamming line. This will increase achievable sDoF per LR if GIA is in the intensive jamming mode.
- **LT/LR density $\rho^{(l)}$:** As Fig. 6(b) shows, larger $\rho^{(l)}$ flattens both the jamming line and aligning curve, which reduces achievable sDoF per LR.

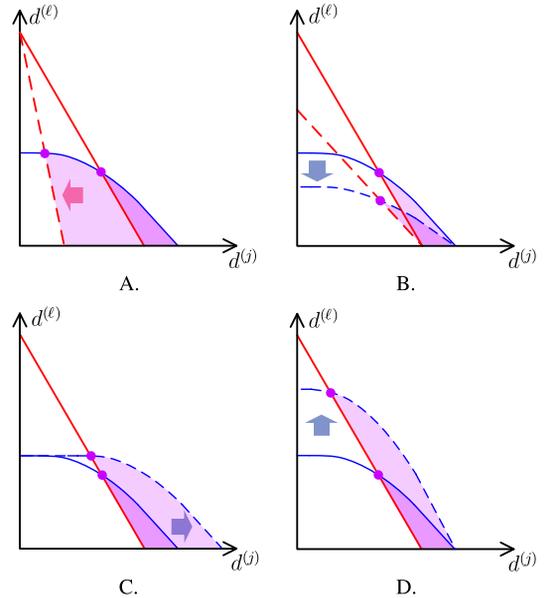


Fig. 6. Illustration of how the feasible region of $(d^{(j)}, d^{(l)})$ changes w.r.t. to network parameters. (a) Larger $\rho^{(j)}$; (b) Larger $\rho^{(l)}$; (c) Larger $M^{(j)}$; (d) Larger $M^{(l)} + N^{(l)}$.

- **LJ antenna $M^{(j)}$:** As Fig. 6(c) shows, larger $M^{(j)}$ pushes the aligning line to the right. This will benefit achievable sDoF per LR if GIA is in the intensive jamming mode.
- **Sum of LT and LR antenna $M^{(l)} + N^{(l)}$:** As Fig. 6(d) shows, larger $M^{(l)} + N^{(l)}$ pushes up the aligning curve, and hence increases achievable sDoF per LR. \square

V. SIMULATION RESULTS

A. Secrecy Rate Under Different Strategies

First compare the secrecy rate (defined in (2)) achieved by the proposed GIA technique with the following three baselines.

- **Cooperative jamming (CJ):** The LTs and LR adopt random transceivers, and the LJs adopt zero-forcing (ZF) precoders to cancel their interference with the LR.
- **Pure IA (IA):** The LTs and LR adopt IA to cancel interference. The LJs remain idle.
- **IA with artificial noise (IAN):** The LTs and LR adopt IA to cancel interference. The LJs generate artificial noise by adopting random precoders.

To verify the legitimacy of the pathloss model proposed in (10), the secrecy rates under channel models with and without pathloss cutoff are simulated.

Fig. 7 illustrates that the proposed GIA technique achieves significant performance gain over the baselines. This is because GIA fully exploits the capability of all legitimate partners to create different amounts of interference at the LR and ER. From the slope of the secrecy rate under GIA technique, it can be seen that the sDoF per node is around 0.9. It is not exactly 1 due to the uncertainty term in (27). Also, it can be seen that the secrecy rate under the two types of channel models are reasonably close.

B. Width of the Transitory Region

Fig. 8 illustrates the sDoF per node D^S as a function of the indicator R under different network densities. If the region in

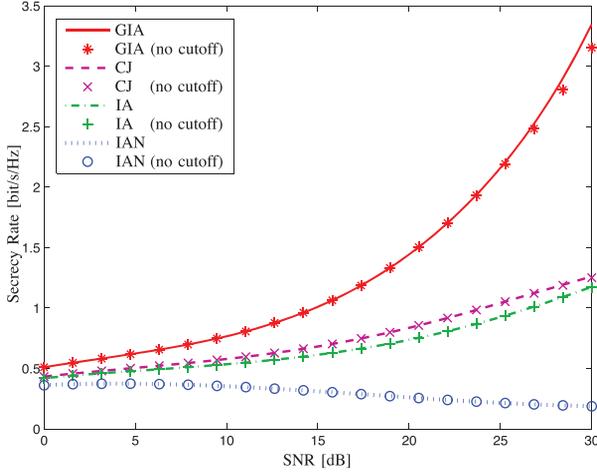


Fig. 7. Secrecy rate as a function of SNR under different schemes. The network parameters are given by $\alpha = 4$, $\theta = 10^{-2}$, $\lambda^{(\ell)} = 4 \times 10^{-2}$, $\lambda^{(j)} = 9 \times 10^{-2}$, $M^{(\ell)} = M^{(j)} = 16$, $N^{(\ell)} = 8$, $N^{(e)} = 32$, and $d^{(\ell)} = d^{(j)} = 1$. The distance between an LT and the associated LR and ER are given by $\|\Delta \mathbf{a}^{(\ell)}\| = 1$ and $\|\Delta \mathbf{a}^{(e)}\| = 1.5$, respectively.

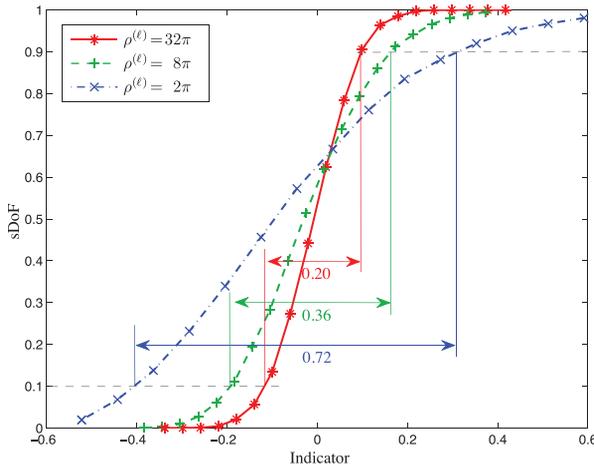


Fig. 8. sDoF per node D^S as a function of the performance indicator R under different user densities. The network parameters are given by $\alpha = 4$, $\theta = 10^{-2}$, and $d^{(\ell)} = d^{(j)} = 1$. The node density is given by $\lambda^{(\ell)} = \lambda^{(j)} = 32 \times 10^{-2}$, $\lambda^{(\ell)} = \lambda^{(j)} = 8 \times 10^{-2}$, and $\lambda^{(\ell)} = \lambda^{(j)} = 2 \times 10^{-2}$ for the three curves, respectively; then fix $M^{(\ell)}$, $M^{(e)}$, $N^{(e)}$ and modify $N^{(\ell)}$ to change the indicator R .

which $D^S \in [0.1, 0.9] \cdot d^{(\ell)}$ is used to represent the transition region, one can see that the width of this region scales on $\mathcal{O}\left(\sqrt{\frac{1}{\rho^{(\ell)}}}\right)$. This fact fits the trend described in Remark 4.1.

C. Resource Allocation Between Transmitting and Jamming

So far, LTs and LJs are assumed to have a fixed prior role. However, their respective roles may overlap. As illustrated in Fig. 9, if part of the LRs are deactivated, then from the point of view of the remaining network nodes, the corresponding LTs effectively become LJs. This conversion empowers the possibility of allocating resources between transmitting and jamming. The comparison between the left and right columns of Fig. 9 sketches the effect of allocating resources between transmitting and jamming. This effect can also be interpreted from

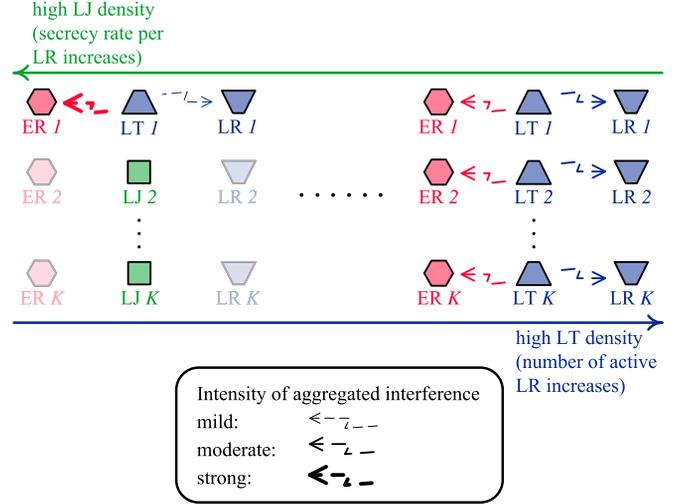


Fig. 9. Effects of the resource allocation between transmitting and jamming.

Fig. 6. The operation of turning LTs to LJs is equivalent to an increase $\rho^{(j)}$ and decrease $\rho^{(\ell)}$. From Fig. 6(a) and (b), this operation enlarges the feasible region and hence increases the sDoF per node at a cost of having less active LRs.

Fig. 10 illustrates the effect of resource allocation between transmitting and jamming. We fix the sum of the density of the LTs and LJs, i.e., $\lambda^{(\ell)} + \lambda^{(j)}$, and illustrate the sDoF per node D^S , or per unit area $D^S \lambda^{(\ell)}$ as functions of the density of LTs $\lambda^{(\ell)}$ (note that this is also the density of active LRs). Under each active LR density, all the possible stream combinations $(d^{(j)}, d^{(\ell)})$ are exhaustively searched to pick out the combination that gives the highest D^S . From the right sub-figure of Fig. 10, in terms of sDoF per unit area, one can roughly separate the operation region into two parts, namely the sparse region and the crowded region. In the sparse region, the benefit from more active LRs dominates, and hence the sDoF per unit area $D^S \lambda^{(\ell)}$ increases under larger $\lambda^{(\ell)}$.⁷ In the crowded region, the loss from smaller sDoF per node D^S dominates, and hence $D^S \lambda^{(\ell)}$ becomes a decreasing function of $\lambda^{(\ell)}$. Therefore, in practice, it is important to control active LR density so that the network operates in a favorable region.

VI. SUMMARY

By creating strong interference at the ERs but little or no interference at the LRs, the GIA technique provides an effective tool for wireless secrecy protection. Based on the theoretical framework established in Part I, Part II offers a design for GIA algorithms that is applicable to large-scale networks and characterizes the performance of this algorithm in stochastic wireless-tap networks. Working modes of GIA have been identified and simple insights into how network parameters affect the performance of wireless-tap networks have been obtained. Numerical results illustrate the contribution of GIA in wireless secrecy protection and confirm the insights.

⁷This fact is not always true due to the discrete choices of $(d^{(j)}, d^{(\ell)})$. For instance, the steep drop indicated in the figure occurs when $d^{(\ell)}$ changes from 2 to 1.

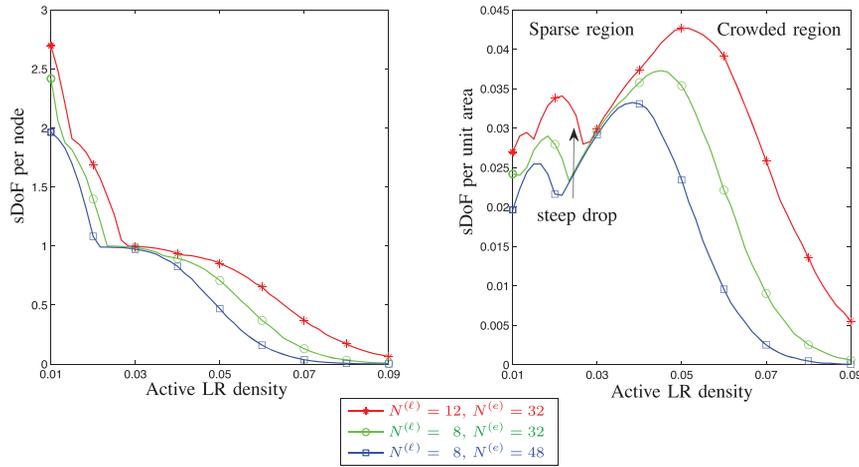


Fig. 10. sDoF per node/unit area as a function of active LR density $\lambda^{(\ell)}$. The network parameters are given by $\alpha = 4$, $\theta = 10^{-2}$, $\lambda^{(\ell)} \in [1 \times 10^{-2}, 9 \times 10^{-2}]$, $\lambda^{(j)} = 13 \times 10^{-2} - \lambda^{(\ell)}$, and $M^{(\ell)} = M^{(j)} = 16$.

APPENDIX A PROOF OF THEOREM 3.1

From Theorem 4.4 of Part I, one only need to show that matrix \mathbf{H}_{all} (defined in Fig. 4 of Part I) is full row-rank. Suppose Problem 2.1 is feasible under alignment subsets $\{\mathcal{A}^{(r)}(k)\}$ and $\{\mathcal{A}^{(t)}(j)\}$. If the intersection of some alignment subsets are non-empty, e.g., $\mathcal{A}^{(r)}(k) \cap \mathcal{A}^{(t)}(j) \neq \emptyset$, then non-overlapping alignment subset $\tilde{\mathcal{A}}^{(r)}(k) = \mathcal{A}^{(r)}(k) \setminus (\mathcal{A}^{(r)}(k) \cap \mathcal{A}^{(t)}(j))$ can be generated. From Corollary 4.1 of Part I, since this operation does not change the alignment set \mathcal{A} , the feasibility of Problem 2.1 is preserved. Hence, to prove the theorem, it is sufficient to consider the case in which

$$\mathcal{A}^{(r)}(k) \cap \mathcal{A}^{(t)}(j) = \emptyset, \quad \forall k, j. \quad (28)$$

From (9) and (28), every $(k, j) \in \mathcal{A}$ belongs to one and only one alignment subset. Hence, one can reorder the rows of \mathbf{H}_{all} and rewrite the matrix as

$$\tilde{\mathbf{H}}_{\text{all}} + \tilde{\tilde{\mathbf{H}}}_{\text{all}}, \quad (29)$$

where

$$\tilde{\mathbf{H}}_{\text{all}} = \text{diag}(\mathbf{H}_1^{\text{U}}, \mathbf{H}_2^{\text{U}}, \dots, \mathbf{H}_K^{\text{U}}, \mathbf{H}_1^{\text{V}}, \mathbf{H}_2^{\text{V}}, \dots, \mathbf{H}_{\tilde{K}}^{\text{V}})$$

with

$$\mathbf{H}_k^{\text{U}} = \begin{bmatrix} \mathbf{H}_{kj_1}^{\text{U}} \\ \mathbf{H}_{kj_2}^{\text{U}} \\ \vdots \\ \mathbf{H}_{kj_S}^{\text{U}} \end{bmatrix}, \quad (k, j_s) \in \mathcal{A}^{(r)}(k), \quad S = |\mathcal{A}^{(r)}(k)|, \quad (30)$$

$$\mathbf{H}_j^{\text{V}} = \begin{bmatrix} \mathbf{H}_{k_1j}^{\text{V}} \\ \mathbf{H}_{k_2j}^{\text{V}} \\ \vdots \\ \mathbf{H}_{k_Sj}^{\text{V}} \end{bmatrix}, \quad (k_s, j) \in \mathcal{A}^{(t)}(j), \quad S = |\mathcal{A}^{(t)}(j)|, \quad (31)$$

and the submatrices in $\tilde{\tilde{\mathbf{H}}}_{\text{all}}$ are given by

$$\mathbf{H}_{kj}^{\text{U}} : (k, j) \notin \mathcal{A}^{(r)}(k), \quad \text{and} \quad \mathbf{H}_{kj}^{\text{V}} : (k, j) \notin \mathcal{A}^{(t)}(j). \quad (32)$$

Substituting the condition of proper alignment subset, i.e., (8), to the expressions of $\mathbf{H}_{kj}^{\text{U}}$ and $\mathbf{H}_{kj}^{\text{V}}$, i.e., (9) and (10) of Part I, we get that matrices \mathbf{H}_k^{U} and \mathbf{H}_j^{V} in (30) and (31) are full row-rank almost surely. Hence, $\tilde{\mathbf{H}}_{\text{all}}$ is full row-rank almost surely.

Moreover, from (9) and (10) of Part I, the elements in different submatrices $\mathbf{H}_{kj}^{\text{U}}$, $\mathbf{H}_{kj}^{\text{V}}$ are independent. Hence (32) assures that $\tilde{\mathbf{H}}_{\text{all}}$ is independent of $\tilde{\tilde{\mathbf{H}}}_{\text{all}}$. Therefore, from (29), \mathbf{H}_{all} is full row-rank almost surely. This completes the proof.

APPENDIX B PROOF OF LEMMA 4.1

As the entries of the channel matrices are independent random variables drawn from continuous distributions, with probability 1, $r^{(\ell)} = S^{(\ell)} \log_2(P) + \mathcal{O}(\log_2 P)$. Substituting this result to (2),

$$R^S = [S^{(\ell)} - S^{(e)}]^+ \log_2(P) + \mathcal{O}(\log_2 P) \quad (33)$$

Substituting (33) to (4), (18) is obtained. In the following, the expression of $S^{(\ell)}$ and $S^{(e)}$ will be derived.

If a link between LR \mathbf{a} and LT (or LJ) \mathbf{b} has zero pathloss, i.e., $L(\mathbf{a}, \mathbf{b}) = 0$, or $(\mathbf{a}, \mathbf{b}) \in \mathcal{A}$, there is no interference on this link. Otherwise, the channel state $\mathbf{H}_{\mathbf{a}, \mathbf{b}}^{(\ell)}$ is independent of $\mathbf{U}_{\mathbf{a}}^{(\ell)}$, $\mathbf{V}_{\mathbf{b}}$.

In this case, $\text{Rn}((\mathbf{U}_{\mathbf{a}}^{(\ell)})^\dagger \mathbf{H}_{\mathbf{a}, \mathbf{b}} \mathbf{V}_{\mathbf{b}}) = \min\{d^{(\ell)}, d^{(x)}\}$ almost surely, where $x = \ell$ for LTs and $x = j$ for LJs. Hence, with probability 1, $S^{(\ell)}$ is given by (19).

Similarly, as the channel state of the eavesdropping network $\{\mathbf{H}_{\mathbf{e}, \mathbf{b}}^{(e)}\}$ is independent of precoders $\{\mathbf{V}_{\mathbf{b}}\}$, (20) is obtained.

APPENDIX C PROOF OF LEMMA 4.2

First try to prove (23). Note that

$$\mathcal{A} = (\cup_{\mathbf{a} \in \mathcal{R}^{(\ell)}} \mathcal{A}^{(r)}(\mathbf{a})) \cup (\cup_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathcal{A}^{(t)}(\mathbf{b})) \cup (\cup_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathcal{A}^{(j)}(\mathbf{b})).$$

From (13), the sets $\cup_{\mathbf{a} \in \mathcal{R}^{(\ell)}} \mathcal{A}^{(r)}(\mathbf{a})$, $\cup_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathcal{A}^{(t)}(\mathbf{b})$, and $\cup_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathcal{A}^{(j)}(\mathbf{b})$ do not overlap. Hence,

$$\begin{aligned} & \sum_{\mathbf{b} \in \mathcal{T}^{(x)}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0 \text{ \& } (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}\} \\ &= \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(x)} \\ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(x)}(\mathbf{b})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\} - \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(x)} \\ (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\}, \end{aligned} \quad (34)$$

where $x \in \{\ell, j\}$. Substituting (21) and (34) to (19),

$$S^{(\ell)} = [N^{(\ell)} - I^{(\ell)} - \tilde{\varepsilon}]^+, \quad (35)$$

where

$$\tilde{\varepsilon} = d^{(\ell)} \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(\ell)} \\ (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\} + d^{(j)} \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(j)} \\ (\mathbf{a}, \mathbf{b}) \in \mathcal{A}^{(r)}(\mathbf{a})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\}.$$

From (22), $\tilde{\varepsilon} \leq \varepsilon$. Moreover, from (11) and (14), if $\tilde{\varepsilon} < \varepsilon$, $\{\mathbf{b} \in \mathcal{T}^{(\ell)} \cup \mathcal{T}^{(j)} \setminus \{\mathbf{a} + \mathbf{p}_a\} : L(\mathbf{a}, \mathbf{b}) > 0\} \subseteq \mathcal{A}$, which means $S^{(\ell)} = d^{(\ell)}$. With this fact and (35), (23) is obtained.

From (15), it is easy to see that ε is bounded within $[0, \max\{d^{(j)}, d^{(\ell)}\} - 1]$. Hence, in the following, the focus is on characterizing the mean and variance of $I^{(\ell)}$. Define

$$i^{(x)} \triangleq \sum_{\substack{\mathbf{b} \in \mathcal{T}^{(x)} \\ (\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(x)}(\mathbf{b})}} \mathbb{1}\{L(\mathbf{a}, \mathbf{b}) > 0\}, x \in \{\ell, j\},$$

then

$$I^{(\ell)} = d^{(\ell)} i^{(\ell)} + d^{(j)} i^{(j)}. \quad (36)$$

To analyze the mean and variance of $I^{(\ell)}$, first analyze those of $i^{(x)}$, $x \in \{\ell, j\}$. To achieve this task, a characterization the spatial distribution of LR is needed.

Lemma C.1 (Spatial Distribution of LR): In a stochastic network, as described by Definition 2, the position of the LR is given by a PPP with density $\lambda^{(\ell)}$.

Proof: From the second item in Definition 2, the position of the LR is a transformation of that of the LTs, which is a PPP with density $\lambda^{(\ell)}$. Hence, from [25, Thm. 1.3.9], the position of the LR is also a PPP with density $\lambda(\mathbf{a})$, $\mathbf{a} \in \mathbb{R}^2$, where

$$\lambda(\mathbf{a}) = \int_{\mathbb{R}^2} p(\Delta \mathbf{a}^{(\ell)}) \lambda^{(\ell)} d(\Delta \mathbf{a}^{(\ell)}) = \lambda^{(\ell)}. \quad (37)$$

Here $p(\mathbf{x})$ denotes the probability density function of \mathbf{x} . This completes the proof. \square

First analyze the expectation $i^{(x)}$. For LR \mathbf{a} , the positions of the unassociated LTs are given by a homogeneous PPP with density $\lambda^{(\ell)}$ on $\mathbb{R}^2 \setminus \{\mathbf{a} + \mathbf{p}_a\}$. Hence

$$\begin{aligned} \mathbb{E}\{i^{(x)}\} &= \int_0^{\theta^{-2/\alpha}} 2\pi r \lambda^{(x)} \\ &\times \mathbb{P}\left\{(\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(x)} \mid \mathbf{b} \in \mathcal{T}^{(x)}, \|\mathbf{a} - \mathbf{b}\| = r\right\} dr. \end{aligned} \quad (38)$$

From Lemma C.1,

$$\begin{aligned} &\mathbb{P}\left\{(\mathbf{a}, \mathbf{b}) \notin \mathcal{A}^{(x)} \mid \mathbf{b} \in \mathcal{T}^{(x)}, \|\mathbf{a} - \mathbf{b}\| = r\right\} \\ &= 1 - \mathbb{P}\left\{\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right| \leq m^{(x)} - 1\right\} \\ &= 1 - \frac{\Gamma(m^{(x)}, \pi r^2 \lambda^{(\ell)})}{\Gamma(m^{(x)})}. \end{aligned} \quad (39)$$

$$= 1 - \frac{\Gamma(m^{(x)}, \pi r^2 \lambda^{(\ell)})}{\Gamma(m^{(x)})}. \quad (40)$$

Substitute (40) to (38):

$$\begin{aligned} \mathbb{E}\{i^{(x)}\} &= \pi \theta^{-\frac{4}{\alpha}} \lambda^{(x)} - \frac{2\pi \lambda^{(x)}}{\Gamma(m^{(x)})} \int_0^{\theta^{-2/\alpha}} r \Gamma(m^{(x)}, \pi r^2 \lambda^{(\ell)}) dr \\ &= \rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} \\ &\times \frac{(\rho^{(\ell)} - m^{(x)}) \Gamma(m^{(x)}, \rho^{(\ell)}) - (\rho^{(\ell)})^{m^{(x)}} e^{-\rho^{(\ell)}}}{\Gamma(m^{(x)})}. \end{aligned} \quad (41)$$

From [26, 8.11.2],

$$\lim_{\rho^{(\ell)} \rightarrow +\infty} \frac{(\rho^{(\ell)} - m^{(x)}) \Gamma(m^{(x)}, \rho^{(\ell)}) - (\rho^{(\ell)})^{m^{(x)}} e^{-\rho^{(\ell)}}}{\Gamma(m^{(x)})} = 0. \quad (42)$$

By combining (39), (41), and (42),

$$\begin{aligned} &-\frac{\lambda^{(x)} (\rho^{(\ell)} - m^{(x)}) \Gamma(m^{(x)}, \rho^{(\ell)}) - (\rho^{(\ell)})^{m^{(x)}} e^{-\rho^{(\ell)}}}{\lambda^{(\ell)} \Gamma(m^{(x)})} \\ &= \int_{\theta^{-2/\alpha}}^{+\infty} 2\pi r \lambda^{(x)} \\ &\times \mathbb{P}\left\{\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right| \leq m^{(x)} - 1\right\} dr, \end{aligned}$$

which is a positive, increasing function of $m^{(x)}$. Hence, when $m^{(x)} \leq \rho^{(\ell)}$, $\mathbb{E}\{i^{(x)}\}$ is in interval

$$\begin{aligned} &\left[\rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)}, \rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)} + \frac{\lambda^{(x)} (\rho^{(\ell)})^{\rho^{(\ell)}} e^{-\rho^{(\ell)}}}{\Gamma(\rho^{(\ell)})}\right] \\ &\subseteq \left[\rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)}, \rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)} + \frac{\lambda^{(x)} \sqrt{\rho^{(\ell)}}}{\lambda^{(\ell)} \sqrt{2\pi}}\right]. \end{aligned} \quad (43)$$

Equation (43) is true because, from Stirling's formula [26, 5.11.7],

$$\sqrt{\frac{2\pi}{z}} (z)^z e^{-z} \leq \Gamma(z) \leq \sqrt{\frac{2\pi}{z}} (z)^z e^{-z} \left(1 + \frac{1}{12z}\right) \quad (44)$$

Further noting that $\mathbb{E}\{i^{(x)}\}$ is a nonnegative decreasing function of $m^{(x)}$, $\mathbb{E}\{i^{(x)}\}$ is in interval

$$\left[\left[\rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)}\right]^+, \left[\rho^{(x)} - \frac{\lambda^{(x)}}{\lambda^{(\ell)}} m^{(x)}\right]^+ + \frac{\lambda^{(x)} \sqrt{\rho^{(\ell)}}}{\lambda^{(\ell)} \sqrt{2\pi}}\right]. \quad (45)$$

We next bound the variance of $i^{(x)}$.

Lemma C.2 (Bound of the Variance of the Sum of Random Variables): $\{x_1, \dots, x_n\}$ are random variables in \mathbb{R} . Then

$$\mathbb{S}\left\{\sum_{i=1}^n x_i\right\} \leq \sum_{i=1}^n \mathbb{S}\{x_i\}. \quad (46)$$

Proof: Denote $\bar{x}_i = \mathbb{E}\{x_i\}$, then

$$\begin{aligned} \mathbb{V}\left\{\sum_{i=1}^n x_i\right\} &= \sum_{i=1}^n \sum_{j=1}^n \mathbb{E}\{(x_i - \bar{x}_i)(x_j - \bar{x}_j)\} \\ &\leq \sum_{i=1}^n \sum_{j=1}^n \sqrt{\mathbb{E}\{(x_i - \bar{x}_i)^2\} \mathbb{E}\{(x_j - \bar{x}_j)^2\}} \end{aligned} \quad (47)$$

$$= \left(\sum_{i=1}^n \mathbb{S}\{x_i\}\right)^2, \quad (48)$$

where (47) is true due to the Cauchy-Schwarz inequality. This completes the proof. \square

From Lemma C.2,

$$\begin{aligned} & \mathbb{S}\{i^{(x)}\} \\ & \leq \int_0^{\theta^{-2/\alpha}} 2\pi r \lambda^{(x)} \mathbb{S}\left(\mathbb{P}\left\{\left(\mathbf{a}, \mathbf{b}\right) \notin \mathcal{A}^{(x)} \mid \mathbf{a} \in \mathcal{R}^{(\ell)}, \right. \right. \\ & \quad \left. \left. \mathbf{b} \in \mathcal{T}^{(x)}, \|\mathbf{a} - \mathbf{b}\| = r\right\}\right) dr \\ & = \int_0^{\theta^{-2/\alpha}} 2\pi r \lambda^{(x)} \\ & \quad \times \mathbb{S}\left(\mathbb{P}\left\{\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right| \geq m^{(x)}\right\}\right) dr, \end{aligned} \quad (49)$$

where function $\mathbb{S}(p) = \sqrt{p(1-p)}$, $p \in [0, 1]$.

Denote

$$\mathbb{P}\left(r, m^{(x)}\right) = \mathbb{P}\left\{\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right| \geq m^{(x)}\right\}.$$

If $m^{(x)} = 0$, $\mathbb{P}(r, m^{(x)}) = 1$, $\forall r \geq 0$. Hence $\mathbb{V}\{i^{(x)}\} = 0$. Otherwise, when $m^{(x)} \geq 1$, $\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right|$ follows Poisson distribution with mean $\pi r^2 \lambda^{(\ell)}$. Hence, from Chernoff inequality,

$$\begin{cases} \mathbb{P}\left(r, m^{(x)}\right) \leq \frac{e^{-\pi r^2 \lambda^{(\ell)}} (e\pi r^2 \lambda^{(\ell)})^{m^{(x)}}}{(m^{(x)})^{m^{(x)}}}, \\ \text{when : } r \leq R = \sqrt{\frac{m^{(x)}}{\pi \lambda^{(\ell)}}}, \\ \mathbb{P}\left(r, m^{(x)}\right) \geq 1 - \frac{e^{-\pi r^2 \lambda^{(\ell)}} (e\pi r^2 \lambda^{(\ell)})^{m^{(x)}}}{(m^{(x)})^{m^{(x)}}}, \\ \text{when : } r \geq R. \end{cases} \quad (50)$$

Then $\mathbb{S}\{i^{(x)}\}$ will be bounded by separating the operation region into the following two cases:

Case 1: $R \leq \theta^{-2/\alpha}$ (i.e., $m^{(x)} \leq \rho^{(\ell)}$). Substitute (50) into (49), noting that $\mathbb{S}(p) \leq \min\{\sqrt{p}, \sqrt{1-p}\}$, then

$$\begin{aligned} \mathbb{S}\{i^{(x)}\} & \leq 2\pi \lambda^{(x)} \left(\int_0^R r \mathbb{S}\left(\mathbb{P}\left(r, m^{(x)}\right)\right) dr \right. \\ & \quad \left. + \int_R^{\theta^{-2/\alpha}} r \mathbb{S}\left(\mathbb{P}\left(r, m^{(x)}\right)\right) dr \right) \\ & \leq 2\pi \lambda^{(x)} \int_0^{\theta^{-2/\alpha}} \frac{r e^{-\frac{\pi r^2 \lambda^{(\ell)}}{2}} (e\pi r^2 \lambda^{(\ell)})^{\frac{m^{(x)}}{2}}}{(m^{(x)})^{\frac{m^{(x)}}{2}}} dr \\ & \leq -2\pi \lambda^{(x)} \frac{(2e)^{\frac{m^{(x)}}{2}} \Gamma\left(\frac{m^{(x)}}{2} + 1, \frac{\pi \lambda^{(\ell)} r^2}{2}\right)}{\pi \lambda^{(\ell)} (m^{(x)})^{\frac{m^{(x)}}{2}}} \Big|_0^{+\infty} \\ & \leq \frac{4\lambda^{(x)} \sqrt{\pi m^{(x)}}}{\lambda^{(\ell)}} \left(1 + \frac{1}{6m^{(x)}}\right), \end{aligned} \quad (51)$$

where last inequality is true because of (44).

Case 2: $R > \theta^{-2/\alpha}$ (i.e., $m^{(x)} > \rho^{(\ell)}$). First, prove the following lemma.

Lemma C.3: When $r \in [0, \tilde{R}]$, $\mathbb{P}(r, m^{(x)}) \leq \frac{1}{2}$, where

$$\tilde{R} = \sqrt{\frac{m^{(x)} - \frac{1}{3}}{\pi \lambda^{(\ell)}}}.$$

Proof: Since $\left|\left\{\mathbf{a}' : \mathbf{a}' \in \mathcal{R}^{(\ell)}, \|\mathbf{a}' - \mathbf{b}\| < r\right\}\right|$ is Poisson random variable with mean $\pi r^2 \lambda^{(\ell)}$, from [27, Thm. 2], when $\pi r^2 \lambda^{(\ell)} + \frac{1}{3} \leq m^{(x)}$, $\mathbb{P}(r, m^{(x)}) \leq \frac{1}{2}$. This completes the proof. \square

Lemma C.4: When $r \in (\tilde{R}, R]$ and $\rho^{(\ell)} \geq \frac{2}{3}$,

$$f(r, \rho^{(\ell)}) \triangleq \frac{e^{-\pi r^2 \lambda^{(\ell)}} (e\pi r^2 \lambda^{(\ell)})^{\rho^{(\ell)}}}{(\rho^{(\ell)})^{\rho^{(\ell)}}} > \frac{1}{2}.$$

Proof: Note that when $r \leq R$,

$$\frac{\partial f}{\partial r} = \frac{e^{-\pi r^2 \lambda^{(\ell)}} (e\pi r^2 \lambda^{(\ell)})^{\rho^{(\ell)}}}{(\rho^{(\ell)})^{\rho^{(\ell)}}} \left(-2\pi r \lambda^{(\ell)} + \frac{2\rho^{(\ell)}}{r}\right) \geq 0, \quad (52)$$

it can be seen that when $r \in (\tilde{R}, R]$,

$$f(r, \rho^{(\ell)}) > f(\tilde{R}, \rho^{(\ell)}) > e^{\rho^{(\ell)} \ln\left(1 - \frac{1}{3\rho^{(\ell)}}\right)}. \quad (53)$$

Noting that $\rho^{(\ell)} \geq \frac{2}{3}$,

$$\begin{aligned} \frac{\partial \rho^{(\ell)} \ln\left(1 - \frac{1}{3\rho^{(\ell)}}\right)}{\partial \rho^{(\ell)}} & = \ln\left(1 - \frac{1}{3\rho^{(\ell)}}\right) + \frac{1}{3\rho^{(\ell)} - 1} \\ & > -\sum_{n=1}^{+\infty} \left(\frac{1}{3\rho^{(\ell)}}\right)^n + \frac{1}{3\rho^{(\ell)} - 1} = 0 \end{aligned} \quad (54)$$

Substitute (54) to (53), then

$$f(r, \rho^{(\ell)}) > f(\tilde{R}, \frac{2}{3}) > \left(1 - \frac{1}{2}\right)^{\frac{2}{3}} > \frac{1}{2}.$$

This completes the proof. \square

With the two lemmas proved above, it can be seen that

$$\begin{aligned} \mathbb{S}\{i^{(x)}\} & \leq 2\pi \lambda^{(x)} \left(\int_0^{\min\{\tilde{R}, \theta^{-2/\alpha}\}} r \mathbb{S}\left(\mathbb{P}\left(r, m^{(x)}\right)\right) dr \right. \\ & \quad \left. + \int_{\min\{\tilde{R}, \theta^{-2/\alpha}\}}^{\theta^{-2/\alpha}} r \mathbb{S}\left(\mathbb{P}\left(r, m^{(x)}\right)\right) dr \right) \\ & \leq 2\pi \lambda^{(x)} \left(\int_0^{\min\{\tilde{R}, \theta^{-2/\alpha}\}} r \mathbb{S}\left(\mathbb{P}\left(r, \rho^{(\ell)}\right)\right) dr \right. \\ & \quad \left. + \int_{\min\{\tilde{R}, \theta^{-2/\alpha}\}}^{\theta^{-2/\alpha}} r/2 dr \right) \end{aligned} \quad (55)$$

$$\leq 2\pi \lambda^{(x)} \int_0^{\theta^{-2/\alpha}} \frac{r e^{-\frac{\pi r^2 \lambda^{(\ell)}}{2}} (e\pi r^2 \lambda^{(\ell)})^{\frac{\rho^{(\ell)}}{2}}}{(\rho^{(\ell)})^{\frac{\rho^{(\ell)}}{2}}} dr \quad (56)$$

$$\leq \frac{4\lambda^{(x)} \sqrt{\pi \rho^{(\ell)}}}{\lambda^{(\ell)}} \left(1 + \frac{1}{6\rho^{(\ell)}}\right), \quad (57)$$

where (55) is true because of Lemma C.3 and the facts that

- (a) $\mathbb{P}(r, m^{(x)})$ is a decreasing function of $m^{(x)}$,
- (b) $\mathbb{S}(p) = \sqrt{p(1-p)}$ is an increasing function in $[0, \frac{1}{2}]$, and
- (c) $\mathbb{S}(p) \leq \frac{1}{2}$.

(56) is true because of Lemma C.4 and $m^{(x)} \geq 1$. From (51) and (57),

$$\mathbb{S}\{i^{(x)}\} \leq \frac{4\lambda^{(x)} \sqrt{\pi \min\{m^{(x)}, \rho^{(\ell)}\}}}{\lambda^{(\ell)}} \times \left(1 + \frac{1}{6 \min\{m^{(x)}, \rho^{(\ell)}\}}\right). \quad (58)$$

From (36), (45), and (58), (24) and (25) are obtained.

APPENDIX D PROOF OF THEOREM 4.1

From Lemma 4.1, to characterize D^S , it is necessary to characterize $S^{(\ell)}$ and $S^{(e)}$. Since $S^{(\ell)}$ is addressed by Lemma 4.2, the focus here is on $S^{(e)}$.

Lemma D.1 (Characterization of $S^{(e)}$):

$$S^{(e)} = \min\{d^{(\ell)}, [N^{(e)} - I^{(e)}]_+\},$$

where

$$I^{(e)} = d^{(\ell)} \sum_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\} + d^{(j)} \sum_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\},$$

$$\mathbb{E}\{I^{(e)}\} = \rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)},$$

and

$$\mathbb{V}\{I^{(e)}\} = \rho^{(\ell)} (d^{(\ell)})^2 + \rho^{(j)} (d^{(j)})^2.$$

Proof: The position of LTs and LJs are given by PPPs with density $\lambda^{(\ell)}$ and $\lambda^{(j)}$, respectively. Hence, $\sum_{\mathbf{b} \in \mathcal{T}^{(\ell)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\}$ and $d^{(j)} \sum_{\mathbf{b} \in \mathcal{T}^{(j)}} \mathbb{1}\{L(\mathbf{e}, \mathbf{b}) > 0\}$ are independent random variables following Poisson distribution, with parameters $\rho^{(\ell)}$ and $\rho^{(j)}$, respectively. From the properties of Poisson distribution and (20), Lemma D.1 is proved. \square

Now start the main flow of the proof of Theorem 4.1. When

$$R^{(e)} = 1 - \frac{N^{(e)}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} > \sqrt{\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)})^2 d^{(\ell)}}},$$

from Lemma D.1 and Chebyshev inequality,

$$\begin{aligned} \mathbb{P}\{S^{(e)} \geq 0\} &\leq \frac{\rho^{(\ell)} (d^{(\ell)})^2 + \rho^{(j)} (d^{(j)})^2}{(R^{(e)})^2 (\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)})^2} \\ &< \frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(R^{(e)} \rho^{(\ell)})^2 d^{(\ell)}}. \end{aligned} \quad (59)$$

Otherwise, when $R^{(e)} < -\sqrt{\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)})^2 d^{(\ell)}}}$, noting that $\rho^{(\ell)} \geq 1$,

$$\begin{aligned} \mathbb{P}\{S^{(e)} \geq d^{(\ell)}\} &\geq 1 - \frac{\rho^{(\ell)} (d^{(\ell)})^2 + \rho^{(j)} (d^{(j)})^2}{(R^{(e)} (\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}) + d^{(\ell)})^2} \\ &\geq 1 - \frac{\rho^{(\ell)} (d^{(\ell)})^2 + \rho^{(j)} (d^{(j)})^2}{(R^{(e)} (\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}))^2} \end{aligned}$$

$$\begin{aligned} &+ \frac{2(\rho^{(\ell)} (d^{(\ell)})^2 + \rho^{(j)} (d^{(j)})^2) d^{(\ell)}}{(R^{(e)} (\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}))^3} \\ &\sim 1 - \mathcal{O}\left(\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(R^{(e)} \rho^{(\ell)})^2 d^{(\ell)}}\right). \end{aligned} \quad (60)$$

Similarly, from Lemma 4.2 and Chebyshev inequality, when

$$\begin{aligned} R^{(\ell)} &= \frac{N^{(\ell)} - d^{(\ell)} + \min\{m^{(\ell)} d^{(\ell)}, \rho^{(\ell)} d^{(\ell)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} \\ &+ \frac{\min\{\frac{\lambda^{(j)}}{\lambda^{(\ell)}} m^{(j)} d^{(j)}, \rho^{(j)} d^{(j)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} - 1 \\ &> \sqrt{\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)})^2 d^{(\ell)}}}, \end{aligned}$$

$$\mathbb{P}\{S^{(\ell)} < d^{(\ell)}\} \sim \mathcal{O}\left(\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(R^{(e)} \rho^{(\ell)})^2 d^{(\ell)}}\right), \quad (61)$$

and when $R^{(\ell)} < -\sqrt{\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(\rho^{(\ell)})^2 d^{(\ell)}}}$,

$$\mathbb{P}\{S^{(\ell)} \geq 0\} \sim 1 - \mathcal{O}\left(\frac{\max\{d^{(\ell)}, d^{(j)}\} \max\{\rho^{(\ell)}, \rho^{(j)}\}}{(R^{(e)} \rho^{(\ell)})^2 d^{(\ell)}}\right). \quad (62)$$

Substituting (59)–(62) to (18), (27) is obtained.

APPENDIX E FEASIBLE REGION UNDER HIGH CONNECTION DENSITY When $\rho^{(\ell)} \gg 1$, the feasible streams

$(d^{(j)}, d^{(\ell)}) \in \{0, \dots, M^{(j)}\} \times \{1, 2, \dots, \min\{N^{(\ell)}, M^{(\ell)}\}\}$ need to satisfy

$$R = \min\{R^{(e)}, R^{(\ell)}\} > 0, \quad \text{where} \quad (63)$$

$$R^{(e)} = 1 - \frac{N^{(e)}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}}, \quad (64)$$

$$\begin{aligned} R^{(\ell)} &= \frac{N^{(\ell)} - d^{(\ell)} + \min\{m^{(\ell)} d^{(\ell)}, \rho^{(\ell)} d^{(\ell)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} \\ &+ \frac{\min\{\frac{\rho^{(j)}}{\rho^{(\ell)}} m^{(j)} d^{(j)}, \rho^{(j)} d^{(j)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} - 1. \end{aligned} \quad (65)$$

Define

$$\begin{aligned} \tilde{R}^{(\ell)} &= \frac{N^{(\ell)} + \min\{M^{(\ell)}, \rho^{(\ell)} d^{(\ell)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} \\ &+ \frac{\min\{\rho^{(j)} (M^{(j)} - d^{(j)}) \rho^{(\ell)} d^{(\ell)}, \rho^{(j)} d^{(j)}\}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} - 1. \end{aligned} \quad (66)$$

Since the quantization error of the $[\cdot]$ function is bounded by $(-1, 0]$, by substituting (12) to (65), one gets

$$\left|R^{(\ell)} - \tilde{R}^{(\ell)}\right| \leq \frac{2d^{(\ell)} + \frac{\rho^{(j)}}{\rho^{(\ell)}} d^{(j)}}{\rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)}} \leq \frac{2}{\rho^{(\ell)}}. \quad (67)$$

Hence, the difference between $R^{(\ell)}$ and $\tilde{R}^{(\ell)}$ can be ignored when $\rho^{(\ell)} \gg 1$. Therefore, one can replace $R^{(\ell)}$ by $\tilde{R}^{(\ell)}$ in (63).

After this replacement, (63) is equivalent to the following four inequalities:

$$f_1(d^{(j)}, d^{(\ell)}) = \rho^{(\ell)} d^{(\ell)} + \rho^{(j)} d^{(j)} - N^{(e)} > 0, \quad (68)$$

$$f_2(d^{(j)}, d^{(\ell)}) = \rho^{(\ell)} d^{(\ell)} - N^{(\ell)} - M^{(\ell)} < 0, \quad (69)$$

$$f_3(d^{(j)}, d^{(\ell)}) = (\rho^{(\ell)})^2 (d^{(\ell)})^2 + \rho^{(\ell)} \rho^{(j)} d^{(\ell)} d^{(j)} + \rho^{(j)} (d^{(j)})^2 - (M^{(\ell)} + N^{(\ell)}) \rho^{(\ell)} d^{(\ell)} - M^{(j)} \rho^{(j)} d^{(j)} < 0, \quad (70)$$

$$f_4(d^{(j)}, d^{(\ell)}) = \rho^{(\ell)} \rho^{(j)} d^{(\ell)} d^{(j)} + \rho^{(j)} (d^{(j)})^2 - N^{(\ell)} \rho^{(\ell)} d^{(\ell)} - M^{(j)} \rho^{(j)} d^{(j)} < 0. \quad (71)$$

It is easy to see that $f_1(d^{(j)}, d^{(\ell)}) = 0$ is a line with slope $-\frac{\rho^{(j)}}{\rho^{(\ell)}}$ and intersection $\frac{N^{(e)}}{\rho^{(\ell)}}$, and $f_2(d^{(j)}, d^{(\ell)}) = 0$ is a horizontal line with intersection $\frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}}$. However, as $f_3(d^{(j)}, d^{(\ell)}) = 0$ and $f_4(d^{(j)}, d^{(\ell)}) = 0$ are second order curves, it is difficult to give a simple characterization of the feasible region. On the other hand, noting that

- $f_3(d^{(j)}, d^{(\ell)}) = 0$ passes through points $(M^{(j)}, 0)$, $(0, 0)$, $(0, \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}})$, and

$$\left(\max\{M^{(j)} - M^{(\ell)} - N^{(\ell)}, 0\}, \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}} \right).$$

- $f_4(d^{(j)}, d^{(\ell)}) = 0$ passes through points $(0, 0)$, $(M^{(j)}, 0)$, the following proposition summarizes the property of $f_2(d^{(j)}, d^{(\ell)})$, $f_3(d^{(j)}, d^{(\ell)})$ and $f_4(d^{(j)}, d^{(\ell)})$.

Proposition E.1 (Properties of the Feasible Region): When $M^{(j)} \geq M^{(\ell)} + N^{(\ell)}$, the points $(d^{(j)}, d^{(\ell)})$ in the interior of trapezoid with vertices $(0, 0)$, $(0, \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}})$,

$$\left(M^{(j)} - M^{(\ell)} - N^{(\ell)}, \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}} \right)$$

and $(M^{(j)}, 0)$ satisfy (69)–(71).

Proof: Noting that function $f(x) = \frac{a+x}{b+x}$, with $a, b \geq 0$ and $x \in [0, +\infty)$ is a decreasing function when $f(x) > 1$ (i.e., $a > b$), from (66), $\tilde{R}^{(\ell)}$ is an strictly decreasing function of $d^{(j)}$ and $d^{(\ell)}$ when $\tilde{R}^{(\ell)} > 0$. Further noting that (69)–(71) $\Leftrightarrow \tilde{R}^{(\ell)} > 0$, if (69)–(71) hold for certain data stream configuration $(d^{(j)}, d^{(\ell)})$, then for any $(\tilde{d}^{(j)}, \tilde{d}^{(\ell)})$ satisfying $\tilde{d}^{(j)} \leq d^{(j)}$ and $\tilde{d}^{(\ell)} \leq d^{(\ell)}$, (69)–(71) must hold. Therefore, to prove the proposition, one only need to prove that $f_i(d^{(j)}, d^{(\ell)}) \leq 0$, $i \in \{2, 3, 4\}$ for all points on the line segment with end points $(M^{(j)} - M^{(\ell)} - N^{(\ell)}, \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}})$ and $(M^{(j)}, 0)$. Since on this line segment, $d^{(\ell)} \leq \frac{M^{(\ell)} + N^{(\ell)}}{\rho^{(\ell)}}$, and thus $f_2(d^{(j)}, d^{(\ell)}) \leq 0$. This line segment can be expressed as

$$d^{(\ell)} = \frac{M^{(j)} - d^{(j)}}{\rho^{(\ell)}}, \quad d^{(j)} \in \{M^{(j)} - M^{(\ell)} - N^{(\ell)}, M^{(j)}\}. \quad (72)$$

Substitute (72) into (70) and (71),

$$f_3(d^{(j)}, d^{(\ell)}) = (d^{(j)} - M^{(j)}) (d^{(j)} + N^{(\ell)} + M^{(\ell)} - M^{(j)}),$$

$$f_4(d^{(j)}, d^{(\ell)}) = N^{(\ell)} (d^{(j)} - M^{(j)}).$$

Hence, when $d^{(j)} \in \{M^{(j)} - M^{(\ell)} - N^{(\ell)}, M^{(j)}\}$, $f_i(d^{(j)}, d^{(\ell)}) \leq 0$, $i \in \{3, 4\}$. This completes the proof. \square

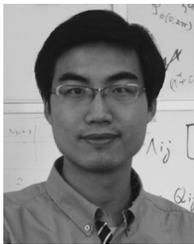
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